

## Quantum field theory

### Conjectured theory $SO(6) = SO(4) \times SO(2) = SU(2) \times SU(2) \times U(1)$

Conjectured [electroweak/dark energy/gravity](http://vixra.org/abs/1111.0111) (<http://vixra.org/abs/1111.0111>) symmetry theory:

$$SO(6) = SO(4) \times SO(2) \\ = SU(2) \times SU(2) \times U(1)$$

If this is true, the Standard Model should be replaced by  $SU(3) \times SO(6)$ . or maybe just  $SO(6)$  if  $SO(6)$  breaks down two ways, once as shown above, and also as in the old Georgi-Glashow  $SU(5)$  grand unified theory (given below), where  $SO(6)$  is isomorphic to  $SU(4)$  which contains the strong force's color charge symmetry,  $SU(3)$ . (See also Table 10.2 in the introduction to group theory for physicists, linked [here](http://astro.sunysb.edu/steinkirch/books/group.pdf) (<http://astro.sunysb.edu/steinkirch/books/group.pdf>.)

Why do we want  $SO(6)$ ? Answer: [Lunsford shows  \$SO\(3,3\) = SO\(6\)\$  unifies gravitation and electrodynamics in 6d.](http://cds.cern.ch/record/688763/files/ext-2003-090.pdf) (<http://cds.cern.ch/record/688763/files/ext-2003-090.pdf>)

$SO(4) = SU(2) \times SU(2)$  is well known as a mathematical isomorphism ([see previous post](http://nige.wordpress.com/2014/06/21/su2-x-su2-so4-and-the-standard-model/) (<http://nige.wordpress.com/2014/06/21/su2-x-su2-so4-and-the-standard-model/>)) as is the fact that  $SO(2) = U(1)$ .

In olden times (circa 1975-84) the media was saturated with the (wrong) prediction of proton decay via the (now long failed) grand unified theory of  $SU(5) = SO(10)$ . The idea was to break down  $SU(5)$  via the  $SO(10)$  isomorphism into  $SO(6) \times SO(4)$ , and from there one of the ideas, namely the isomorphism ([based on the fact that the left force is left-handed so the Yang-Mills  \$SU\(2\)\$  model reduces to a simple single element  \$U\(1\)\$  theory for right-handed spinors:  \$SU\(2, \text{Right}\) = U\(1, \text{Hypercharge}\)\$ \).](https://www.google.co.uk/url?sa=t&rct=j&q=&esrc=s&source=web&cd=4&cad=rja&uact=8&ved=0CDAOFjAD&url=https%3A%2F%2Fwww.ntu.edu.sg%2Fias%2Fupcomingevents%2Fiasppcit%2FDocuments%2FLecture%2520Notes%2FDay8_0950am_HaraldFritsch_GrandUnification.ppt&ei=c0-0U_WTEMHaoOmngOgI&usq=AFOjCNG5YIcwX8ypoYee9-dNWqx7KnAyrO&bvm=bv.70138588.d.ZGU) ([https://www.google.co.uk/url?sa=t&rct=j&q=&esrc=s&source=web&cd=4&cad=rja&uact=8&ved=0CDAOFjAD&url=https%3A%2F%2Fwww.ntu.edu.sg%2Fias%2Fupcomingevents%2Fiasppcit%2FDocuments%2FLecture%2520Notes%2FDay8\\_0950am\\_HaraldFritsch\\_GrandUnification.ppt&ei=c0-0U\\_WTEMHaoOmngOgI&usq=AFOjCNG5YIcwX8ypoYee9-dNWqx7KnAyrO&bvm=bv.70138588.d.ZGU](https://www.google.co.uk/url?sa=t&rct=j&q=&esrc=s&source=web&cd=4&cad=rja&uact=8&ved=0CDAOFjAD&url=https%3A%2F%2Fwww.ntu.edu.sg%2Fias%2Fupcomingevents%2Fiasppcit%2FDocuments%2FLecture%2520Notes%2FDay8_0950am_HaraldFritsch_GrandUnification.ppt&ei=c0-0U_WTEMHaoOmngOgI&usq=AFOjCNG5YIcwX8ypoYee9-dNWqx7KnAyrO&bvm=bv.70138588.d.ZGU)) may be of use to us for recycling purposes (to produce a better theory):

$$SU(5) \\ = SO(10) \\ = SO(6) \times SO(4) \\ = SU(4) \times SU(2, \text{Left}) \times SU(2, \text{Right}) \\ = SU(3) \times SU(2, \text{Left}) \times U(1)$$

Well, maybe we don't need the reduction  $SU(4)$  to  $SU(3)$ , but we do want to consider the symmetry break down of  $SO(6)$  because Lunsford found that group useful:

$$= SO(6) \\ = SO(4) \times SO(2) \\ = SU(2, \text{Left}) \times SU(2, \text{Right}) \times U(1, \text{Dark energy/gravity}) \\ = SU(2, \text{Left}) \times U(1, \text{Hypercharge}) \times U(1, \text{Dark energy/gravity})$$

This is pretty neat because it also fits in with Woit's conjecture that that shows how to obtain the normal electroweak sector charges with their handedness (chiral) features by using a correspondence between the vacuum charge vector and Clifford algebra to represent  $SO(4)$  whose  $U(2)$  symmetry group subset contains the  $2 \times 2 = 4$  particles in one generation of Standard Model quarks or leptons, together with their correct Standard Model charges; [for details see pages 13-17 together with](https://archive.org/stream/arxiv-hep-th0206135/hep-th0206135/page/n50/mode/1up)

[51 of Woit's 2002 paper, \*OFT and Representation Theory\*.](https://archive.org/stream/arxiv-hep-th0206135/hep-th0206135/page/n50/mode/1up) (<https://archive.org/stream/arxiv-hep-th0206135/hep-th0206135/page/n50/mode/1up>)

(It's abstract but when you think about it, you're just using a consistent representation theory to select the 4 elements of the  $U(2)$  matrix from the 16 of  $SO(4)$ . Most of the technical trivia in the paper is superfluous to the key example we're interested in which occurs in the table of page 51. Likewise, when you look compare the elements of the three  $2 \times 2$  Pauli matrices of  $SU(2)$  to the eight  $3 \times 3$  Gell-Mann matrices of  $SU(3)$  you can see that the first three of the  $SU(3)$  matrices are analogous to the three  $SU(2)$  matrices, give or take a global multiplication factor of  $i$ . In other words, you can pictorially see what's going on if you write out the matrices and circle those which correspond to one another.) (<https://archive.org/stream/arxiv-hep-th0206135/hep-th0206135/page/n50/mode/1up>)

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